

# Frictional Forces

*by*

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**P3.2A** Identify the magnitude and direction of everyday forces (e.g., wind, tension in ropes, pushes and pulls, weight).

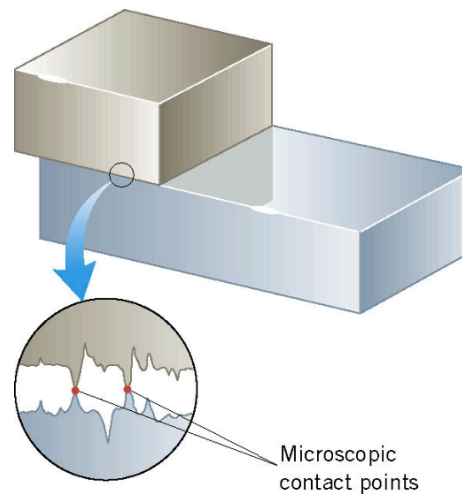
## **There are two types of frictional forces**

1. Static Frictional Force.
2. Kinetic Frictional Kinetic Force.

Frictional forces nearly always act opposite to the direction of motion.

## *Frictional Force*

When an object, in contact with a surface, moves or attempts to move, there is a force acting on that object. The component of this force that is parallel to the surface is called the **frictional force**.



There are only few contact points between two polished surfaces that are in contact.

## Static Frictional Force ( $f_s$ ) in contact- No motion

When the two surfaces, that are in contact, are not sliding across one another the friction is called static friction.

Static frictional force has the symbol  $f_s$

Static frictional force acts opposite to the direction of motion.

The magnitude or value ( $f_s$ ) of the static friction can be calculated when multiplying the coefficient of static friction by the normal force or support force.

*Static Frictional Force*

$$f_s = \mu_s F_N = \mu_s mg$$

$\mu_s$  is the coefficient of static friction ( $0 < \mu_s < 1$ )

$F_N$  is the normal or support force.

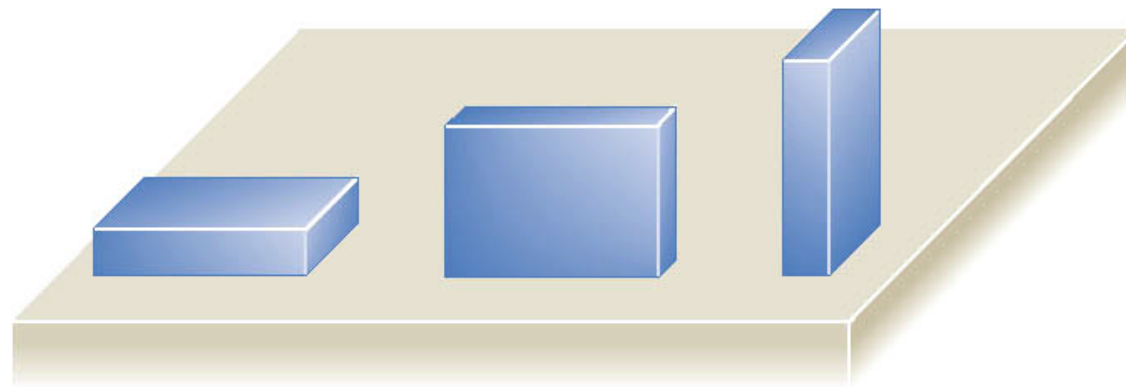
m is the mass,  $g = 9.8 \text{ m/s}^2$

To move an object, you need to pull with a force that is greater than the maximum static frictional force ( $F > f_s^{\text{MAX}}$ ).

Static Frictional Force depends on the mass only.

The static frictional force depend only on the mass and does not depend on the way the mass is in contact with the surface.

So, for the block in contact with the table below, the maximum static frictional force is the same, no matter which side of the block is in contact with the table.



**Example 1:** A box is on a table, and a hand is trying to pull a box with a rope by applying a horizontal force ( $F$ ) as shown in figures a, b and c.



No movement  
(a)



No movement  
(b)



When movement just begins  
(c)

(a)  $F < f_s$ . No movement.

(b)  $F = f_s$ . No movement.

(c)  $F > f_s$ . ( $f_s^{\text{MAX}}$ ). The box just begins to move.

To move an object, you need to pull with a force that is greater than the maximum static frictional force ( $F > f_s^{\text{MAX}}$ ).



## Kinetic Frictional Force in contact

### Opposing the sliding motion

Kinetic frictional force opposes the relative sliding motion between two objects that are in contact. Kinetic frictional force has the symbol ( $f_k$ )

The magnitude (value) of the Kinetic frictional force ( $f_k$ ) can be calculated when multiplying the coefficient of kinetic friction by the normal force or support force.

<i>Kinetic Frictional Force</i>
$f_k = \mu_k F_N = \mu_k mg$

$\mu_k$  is the coefficient of static friction ( $0 < \mu_k < 1$ )

$F_N$  is the normal or support force.

$m$  is the mass,  $g = 9.8 \text{ m/s}^2$

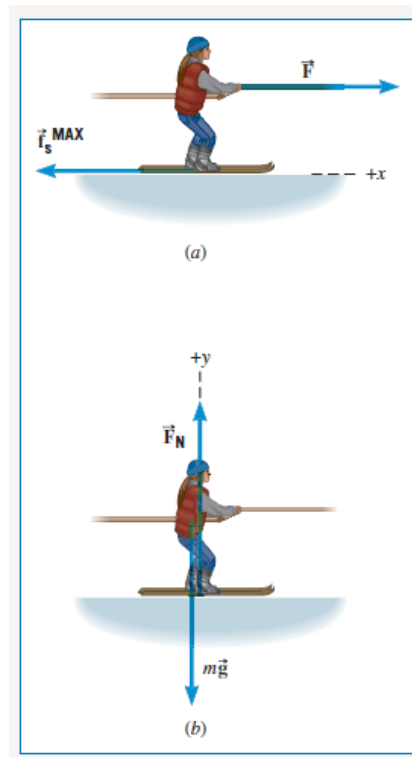
**Table 4.2** Approximate Values of the Coefficients of Friction for Various Surfaces

Materials	Coefficient of Static Friction, $\mu_s$	Coefficient of Kinetic Friction, $\mu_k$
Glass on glass (dry)	0.94	0.4
Ice on ice (clean, 0 °C)	0.1	0.02
Rubber on dry concrete	1.0	0.8
Rubber on wet concrete	0.7	0.5
Steel on ice	0.1	0.05
Steel on steel (dry hard steel)	0.78	0.42
Teflon on Teflon	0.04	0.04
Wood on wood	0.35	0.3

Usually  $\mu_s > \mu_k$

**Example 2:** *The force Needed to Start a Skier Moving.*

A skier standing on snow and holding onto a rope, which is about to pull her with a force  $F$ . The skier mass  $m$  is 59 kg. The coefficient of the static friction between the skier and the snow is  $\mu_s = 0.14$ . What is the maximum force that the tow rope should pull without causing her to move?



$$m = 59 \text{ kg},$$

$$g = 9.8 \text{ m/s}^2,$$

$$\mu_s = 0.14$$

The static frictional force  $f_s^{\text{MAX}}$  can be calculated:

$$\begin{aligned} f_s^{\text{MAX}} &= \mu_s F_N = \mu_s mg \\ &= 0.14 \times 59 \times 9.8 = 81 \text{ N} \end{aligned}$$

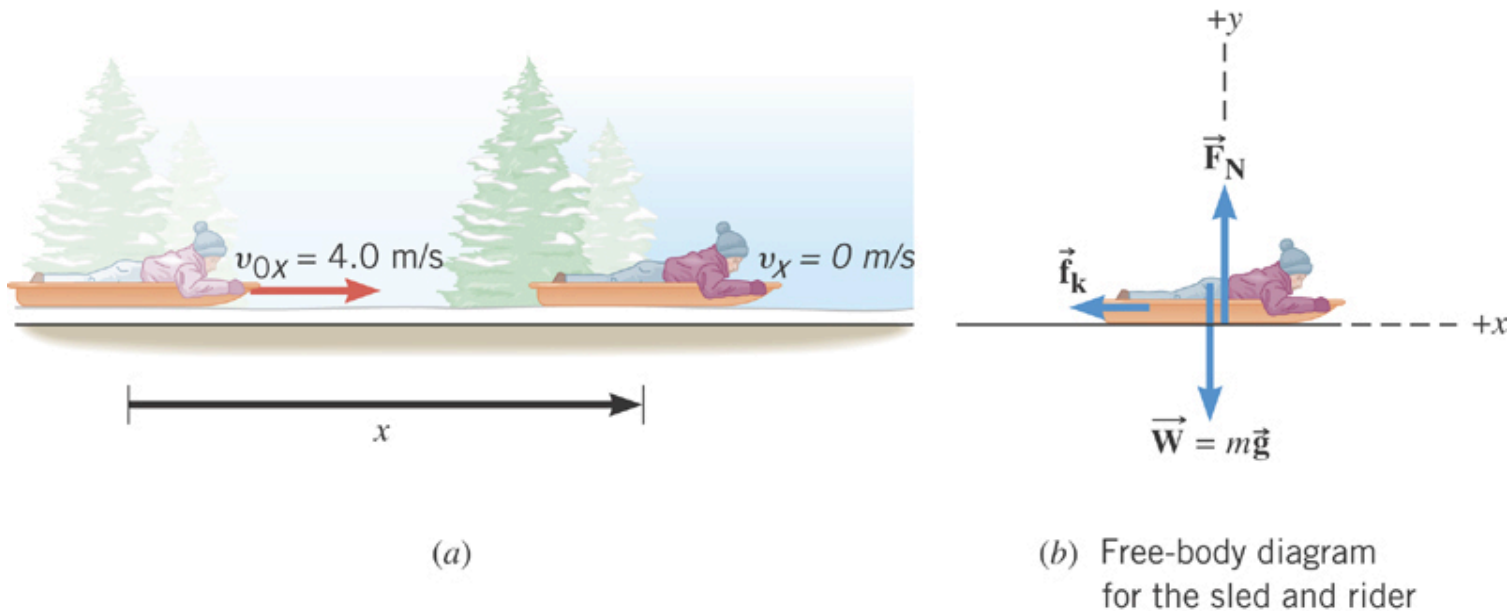
So, the maximum force that the tow rope should pull without causing her to move is 81 N.

For the skier to move forward, the force should pull with more than 81 N.

To move an object, you need to pull with a force that is greater than the maximum static frictional force ( $F > f_s^{\text{MAX}}$ ).

### Example 3: A Sled and a Rider

A sled and a rider are moving at a speed of 4.0 m/s along an horizontal stretch of snow. The snow exerts a kinetic frictional force on the runners of the sled, so the sled slows down and eventually comes to a stop.



The *free-body-diagram* is a diagram that represents the object and the forces that act on it.

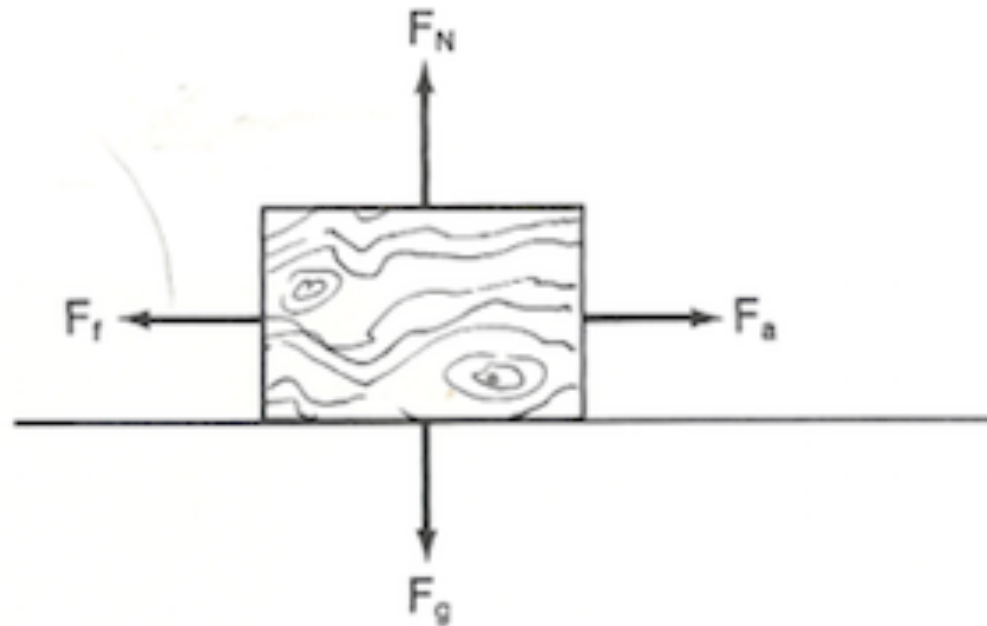
## Sample Problem:

1. It takes 50 N to pull a 6.0 kg object along a desk at a constant speed.

What is the coefficient of friction?

$$\begin{aligned}\mu &= \frac{F_f}{F_N} \\ &= \frac{F_f}{mg} \text{ (since } F_N = F_g = mg\text{)} \\ &= \frac{50 \text{ N}}{(6.0 \text{ kg})(9.8 \text{ N/kg})} \\ &= 0.85\end{aligned}$$

For a block pulled across a rough table top



$F_g$  is the force of gravity on the object.

$F_N$  is the normal force exerted by the table on the block.

$F_a$  is the applied force.

$F_f$  is the force of friction.

2. The coefficient of sliding friction between two materials is 0.35. A 5.0 kg object made of one material is being pulled along a table made of another material. What is the force of friction?

$$\begin{aligned} F_f &= \mu F_N \\ &= \mu mg \quad (\text{since } F_N = F_g = mg) \\ &= (0.35) (5.0 \text{ kg}) (9.8 \text{ N/kg}) \\ &= 17 \text{ N} \end{aligned}$$



## Practice Problems:

1. A 70 kg hockey player glides across the ice on steel skates. What is the force of friction acting on the skater? **Answer 34.3 N**
2. The driver of a 1500 kg car applies the brakes on a concrete road. Calculate the force of friction (a) on a dry road and (b) on a wet road.  
**Answer (a) 11760 N, (b) 7350 N**

## ***References:***

1) Humanic. (2013). [www.physics.ohio-state.edu/~humanic/](http://www.physics.ohio-state.edu/~humanic/). In Thomas Humanic Brochure Page.

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2) Cutnell, J. D. & Johnson, K. W. (1998). *Cutnell & Johnson Physics, Fourth Edition*. New York: John Wiley & Sons, Inc.

*The edition was dedicated to the memory of Stella Kupferberg, Director of the Photo Department: "We miss you, Stella, and shall always remember that a well-chosen photograph should speak for itself, without the need for a lengthy explanation"*

- 3) Martindale, D. G. & Heath, R. W. & Konrad, W. W. & Macnaughton, R. R. & Carle, M. A. (1992). *Heath Physics*. Lexington: D.C. Heath and Company
- 4) Zitzewitz, P. W. (1999). *Glencoe Physics Principles and Problems*. New York: McGraw-Hill Companies, Inc.
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- 6) Nada H. Saab (Saab-Ismail), (2009- 2014) Wayne RESA, Bilingual Department.